#### **Introduction to Bioinformatics**

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### **Course Details**

- Course Code: BLM 3810
- Course Name: Introduction to Bioinformatics
- Credit: 3
- Nature of the course: Lecture
- Course web page:

https://avesis.yildiz.edu.tr/zeyneb/documents

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### **Assesment**

• Midterm : 30%

• Homework : 25%

• Final : 40%

• Attendance & participation : 05%

(The requirement for attendance is 70%)

### **Rules of the Conduct**

- No eating /drinking in class
  - except water
- Cell phones must be kept outside of class or switched-off during class
  - If your cell-phone rings during class or you use it in any way, you will be asked to leave and counted as unexcused absent.
- No web surfing and/or unrelated use of computers,
  - when computers are used in class or lab.

### **Rules of the Conduct**

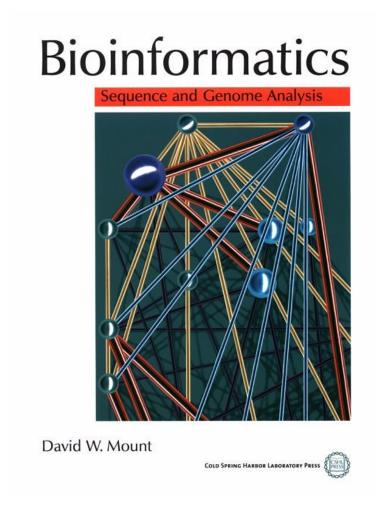
- You are responsible for checking the class web page often for announcements.
  - https://avesis.yildiz.edu.tr/zeyneb/documents
- Academic dishonesty and cheating
  - will not be tolerated
  - will be dealt with according to university rules and regulations
    - <a href="http://www.yok.gov.tr/content/view/475/">http://www.yok.gov.tr/content/view/475/</a>
    - Presenting any work, or a portion thereof, that does not belong to you is also considered academic dishonesty.

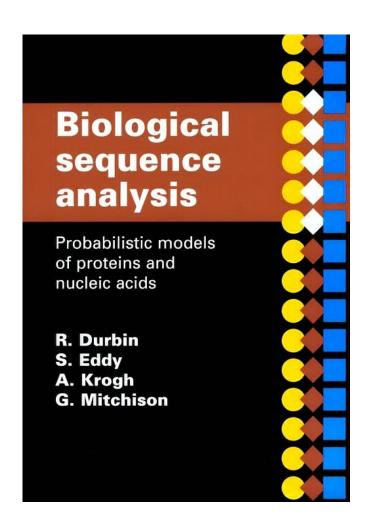
### **Attendance Policy**

- The requirement for attendance is 70%
  - Hospital reports are not accepted to fulfill the requirement for attendance.
  - The students, who fail to fulfill the attendance requirement, will be excluded from the final exams and the grade of F0 will be given.
  - Link for the rules and regulations:

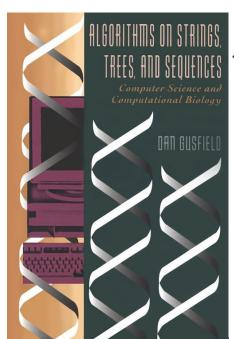
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<a href="http://www.yok.gov.tr/content/view/544/230/lang,tr">http://www.yok.gov.tr/content/view/544/230/lang,tr</a> TR/

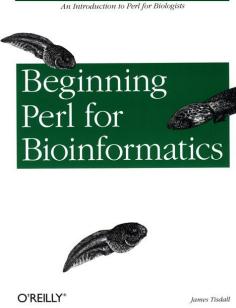
#### **Recommended Texts**

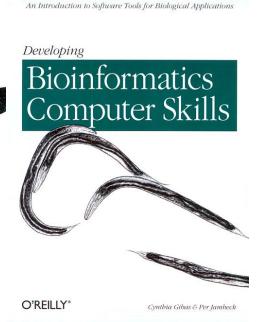


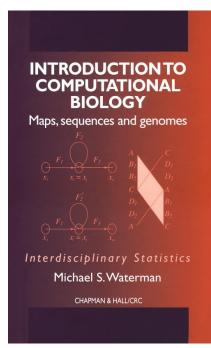


### **Recommended Texts - 2**

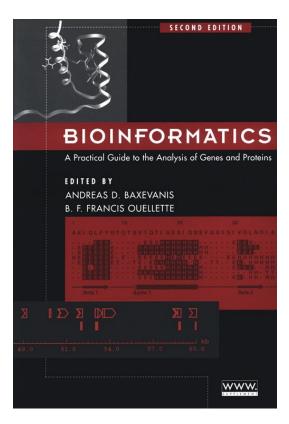


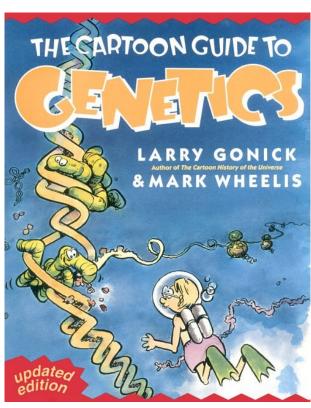


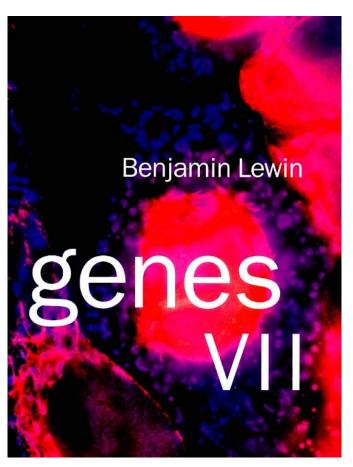




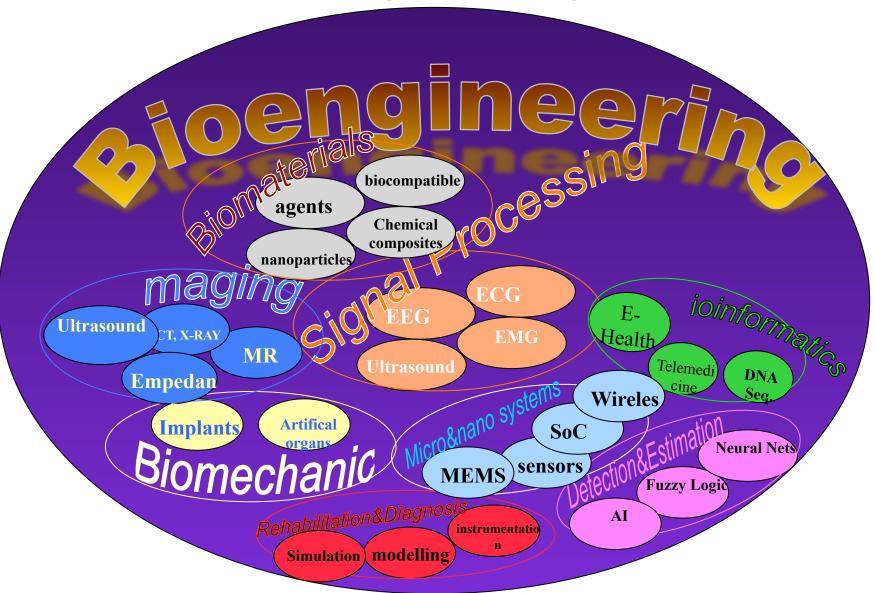
### **Recommended Texts - 3**







# **Bioengineering**



### Bioengineering

- basic research-oriented activity closely related to
  - biotechnology and
  - genetic engineering
    - modification of animal or plant cells to improve plants or animals to develop new micro-organisms
- Bioengineering integrates
  - physical,
  - chemical,
  - mathematical, and
  - computational sciences and
  - engineering principles

to study biology, medicine, behavior, and health.

### Bioengineering

- It advances fundamental concepts;
  - creates knowledge from the molecular to the organ systems levels;
  - develops innovative biologics, materials, processes, implants, devices, and informatics approaches

#### for the

- prevention,
- diagnosis, and
- treatment of disease,

for patient rehabilitation, and for improving health

# Information Systems:

# **Fundamentals**

### **Informatics**

- The term informatics broadly describes the study and practice of
  - creating,
  - storing,
  - finding,
  - manipulating
  - sharing
  - information.

## **Informatics -** Etymology

- In 1956 the German computer scientist Karl Steinbuch coined the word Informatik
  - [Informatik: Automatische Informationsverarbeitung ("Informatics: Automatic Information Processing")]
- The French term informatique was coined in 1962 by Philippe Dreyfus
  - [Dreyfus, Phillipe. L'informatique. Gestion, Paris, June 1962, pp. 240–41]
- The term was coined as a combination of information and automatic to describe the science of automating information interactions

## **Informatics -** Etymology

- The morphology—informat-ion + -ics—uses
- the accepted form for names of sciences,
  - as conics, linguistics, optics,
- or matters of practice,
  - as economics, politics, tactics
- linguistically, the meaning extends easily
  - to encompass both
    - the science of information
    - the practice of information processing.

### **Data - Information - Knowledge**

#### Data

- unprocessed facts and figures without any added interpretation or analysis.
  - {The price of crude oil is \$80 per barrel.}

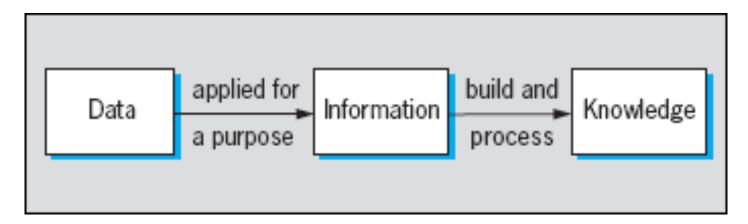
#### Information

- data that has been interpreted so that it has meaning for the user.
  - {The price of crude oil has risen from \$70 to \$80 per barrel}
    - [gives meaning to the data and so is said to be information to someone who tracks oil prices.]

### **Data - Information - Knowledge**

### Knowledge

- a combination of information, experience and insight that may benefit the individual or the organisation.
  - {When crude oil prices go up by \$10 per barrel, it's likely that petrol prices will rise by 2p per litre.}
    - [This is knowledge]
    - [insight: the capacity to gain an accurate and deep understanding of someone or something; an accurate and deep understanding]



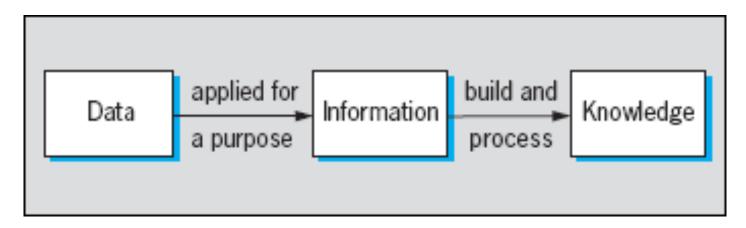
- Data becomes information when it is applied to some purpose and adds value for the recipient.
  - For example a set of raw sales figures is data.
    - For the Sales Manager tasked with solving a problem of poor sales in one region, or deciding the future focus of a sales drive, the raw data needs to be processed into a sales report.
  - It is the sales report that provides information.

- Collecting data is expensive
  - you need to be very clear about why you need it and how you plan to use it.
  - One of the main reasons that organisations collect data is to monitor and improve performance.
    - if you are to have the information you need for control and performance improvement, you need to:
      - collect data on the indicators that really do affect performance
      - collect data reliably and regularly
      - be able to convert data into the information you need.

- To be useful, data must satisfy a number of conditions. It must be:
  - relevant to the specific purpose
  - complete
  - accurate
  - timely
    - data that arrives after you have made your decision is of no value

- in the right format
  - information can only be analysed using a spreadsheet if all the data can be entered into the computer system
- available at a suitable price
  - the benefits of the data must merit the cost of collecting or buying it.
- The same criteria apply to information.
  - It is important
    - to get the right information
    - to get the information right

### Converting information to knowledge



- Ultimately the tremendous amount of information that is generated is only useful if it can be applied to create knowledge within the organisation.
- There is considerable blurring and confusion between the terms information and knowledge.

### Converting information to knowledge

- think of knowledge as being of two types:
  - Formal, explicit or generally available knowledge.
    - This is knowledge that has been captured and used to develop policies and operating procedures for example.
  - Instinctive, subconscious, tacit or hidden knowledge.
    - Within the organisation there are certain people who hold specific knowledge or have the 'know how'
      - {"I did something very similar to that last year and this happened...."}

### Converting information to knowledge

- Clearly, both types of knowledge are essential for the organisation.
- Information on its own will not create a knowledge-based organisation
  - but it is a key building block.
- The right information fuels the development of intellectual capital
  - which in turns drives innovation and performance improvement.

# **DEFINITION(S) OF SYSTEM**

A system can be broadly defined as an integrated set of elements that accomplish a defined objective.

People from different engineering disciplines have different perspectives of what a "system" is.

For example,

software engineers often refer to an integrated set of computer programs as a "system"

electrical engineers might refer to complex integrated circuits or an integrated set of electrical units as a "system"

As can be seen, "system" depends on one's perspective, and the "integrated set of elements that accomplish a defined objective" is an appropriate definition.

### **Definition(s) of system**

- A system is an assembly of parts where:
  - The parts or components are connected together in an organized way.
  - The parts or components are affected by being in the system (and are changed by leaving it).
  - The assembly does something.
  - The assembly has been identified by a person as being of special interest.
- Any arrangement which involves the handling, processing or manipulation of resources of whatever type can be represented as a system.
- Some definitions on online dictionaries
  - http://en.wikipedia.org/wiki/System
  - http://dictionary.reference.com/browse/systems
  - http://www.businessdictionary.com/definition/system.html

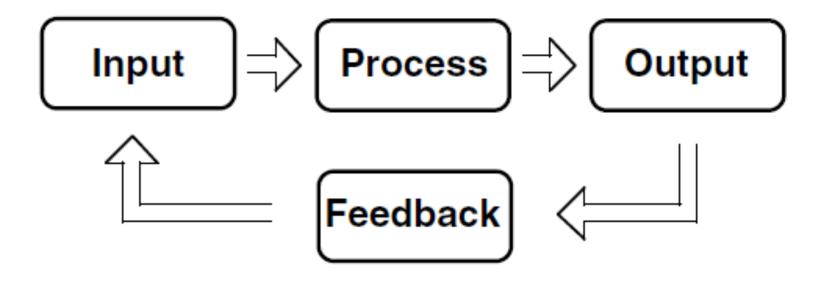
### **Definition(s) of system**

- A system is defined as multiple parts working together for a common purpose or goal.
- Systems can be large and complex
  - such as the air traffic control system or our global telecommunication network.
- Small devices can also be considered as systems
  - such as a pocket calculator, alarm clock, or 10speed bicycle.

### **Definition(s) of system**

- Systems have inputs, processes, and outputs.
- When feedback (direct or indirect) is involved, that component is also important to the operation of the system.
- To explain all this, systems are usually explained using a model.
- A model helps to illustrate the major elements and their relationship, as illustrated in the next slide

### A systems model



### **Information Systems**

- The ways that organizations
  - Store
  - Move
  - Organize
  - Process

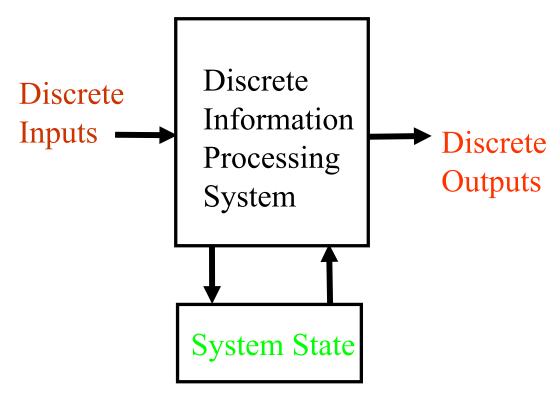
their information

### **Information Technology**

- Components that implement information systems,
  - Hardware
    - physical tools: computer and network hardware, but also low-tech things like pens and paper
  - Software
    - (changeable) instructions for the hardware
  - People
  - Procedures
    - instructions for the people
  - Data/databases

### **Digital System**

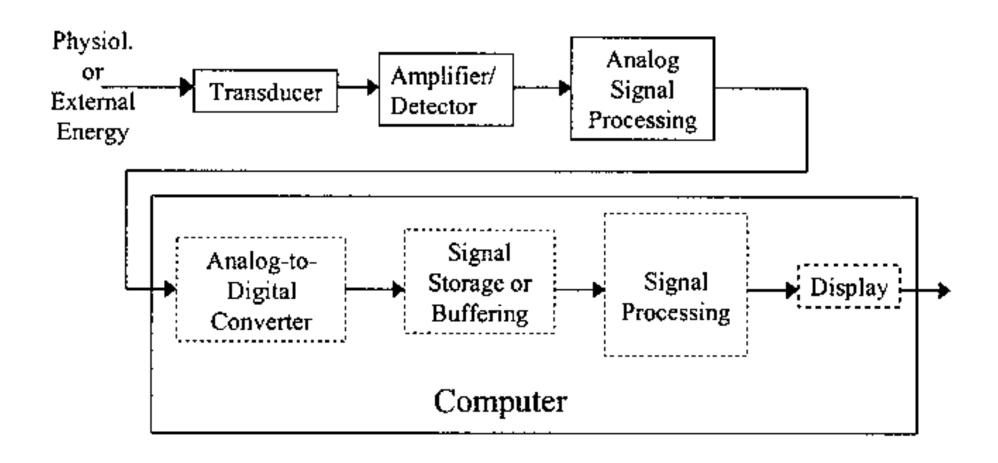
• Takes a set of discrete information (<u>inputs</u>) and discrete internal information (<u>system state</u>) and generates a set of discrete information (<u>outputs</u>).



# Signal

- An information variable represented by physical quantity.
- For digital systems, the variable takes on discrete values.
- Two level, or binary values are the most prevalent values in digital systems.
- Binary values are represented abstractly by:
  - digits 0 and 1
  - words (symbols) False (F) and True (T)
  - words (symbols) Low (L) and High (H)
  - and words On and Off.
- Binary values are represented by values or ranges of values of physical quantities

### A typical measurement system



#### **Transducers**

- A "transducer" is a device that converts energy from one form to another.
- In signal processing applications, the purpose of energy conversion is to transfer information, not to transform energy.
- In physiological measurement systems, transducers may be
  - input transducers (or sensors)
    - they convert a non-electrical energy into an electrical signal.
    - for example, a microphone.
  - output transducers (or actuators)
    - they convert an electrical signal into a non-electrical energy.
    - For example, a speaker.

# Analogue signal

- The analogue signal
  - a continuous variable defined with infinite precision

is converted to a discrete sequence of measured values which are represented digitally

- Information is lost in converting from analogue to digital, due to:
  - inaccuracies in the measurement
  - uncertainty in timing
  - limits on the duration of the measurement
- These effects are called quantisation errors

# Digital signal

• The continuous analogue signal has to be held before it can be sampled

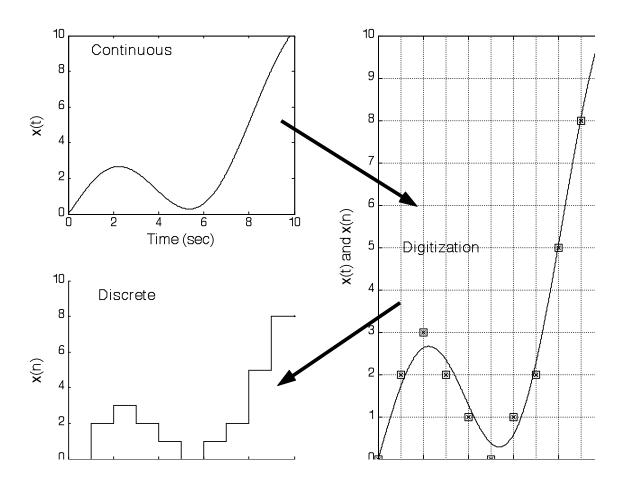
Otherwise, the signal would be changing during the measurement

• Only after it has been held can the signal be measured and the measurement converted to a digital value

#### Signal Encoding: Analog-to Digital Conversion

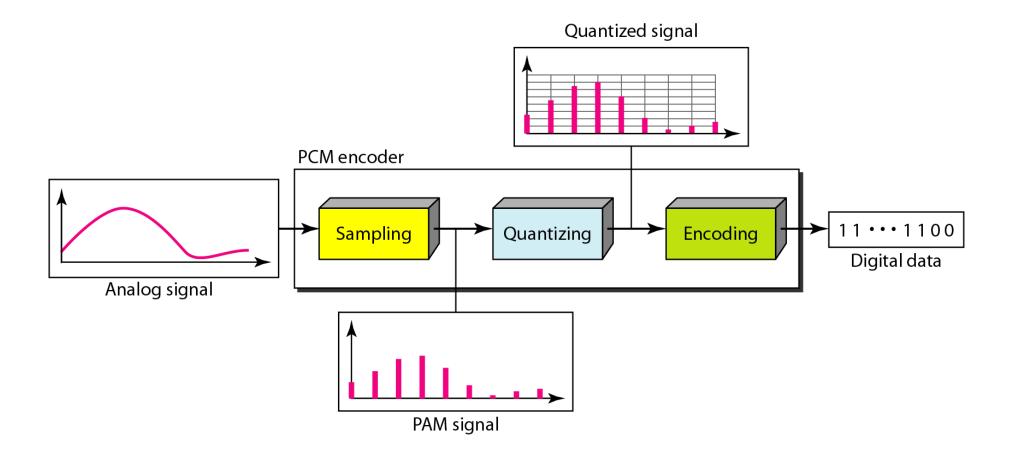
Continuous (analog) signal ←→ Discrete signal

 $x(t) = f(t) \leftrightarrow$  Analog to digital conversion  $\leftrightarrow x[n] = x[1], x[2], x[3], ... x[n]$ 



# **Analog-to Digital Conversion**

- ADC consists of four steps to digitize an analog signal:
  - 1. Filtering
  - 2. Sampling
  - 3. Quantization
  - 4. Binary encoding
- Before we sample, we have to filter the signal to limit the maximum frequency of the signal as it affects the sampling rate.
- Filtering should ensure that we do not distort the signal, ie remove high frequency components that affect the signal shape.

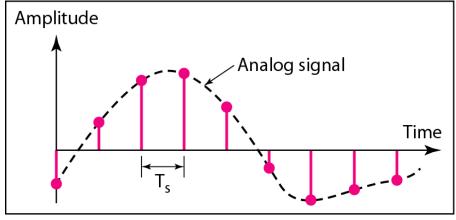


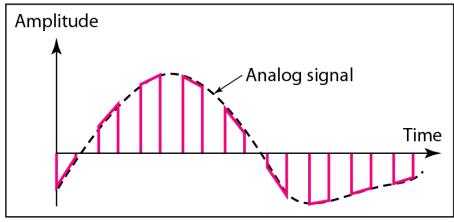
# Sampling

- The sampling results in a discrete set of digital numbers that represent measurements of the signal
  - usually taken at equal intervals of time
- Sampling takes place after the hold
  - The hold circuit must be fast enough that the signal is not changing during the time the circuit is acquiring the signal value
- We don't know what we don't measure
- In the process of measuring the signal, some information is lost

# Sampling

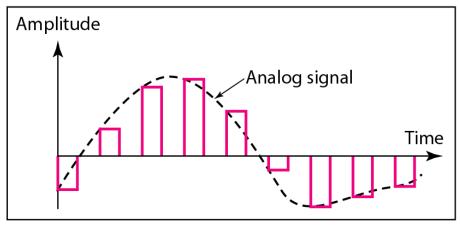
- Analog signal is sampled every T<sub>S</sub> secs.
- T<sub>s</sub> is referred to as the sampling interval.
- $f_s = 1/T_s$  is called the sampling rate or sampling frequency.
- There are 3 sampling methods:
  - Ideal an impulse at each sampling instant
  - Natural a pulse of short width with varying amplitude
  - Flattop sample and hold, like natural but with single amplitude value
- The process is referred to as pulse amplitude modulation PAM and the outcome is a signal with analog (non integer) values





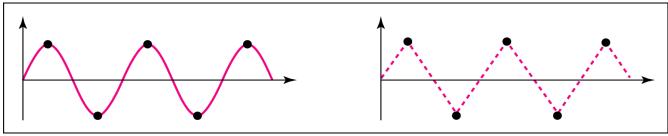
a. Ideal sampling

b. Natural sampling

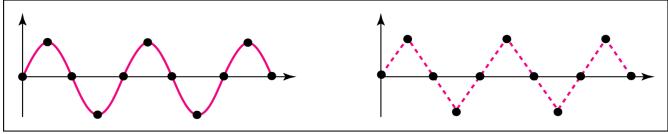


c. Flat-top sampling

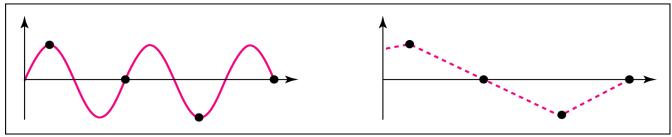
#### Recovery of a sampled sine wave for different sampling rates



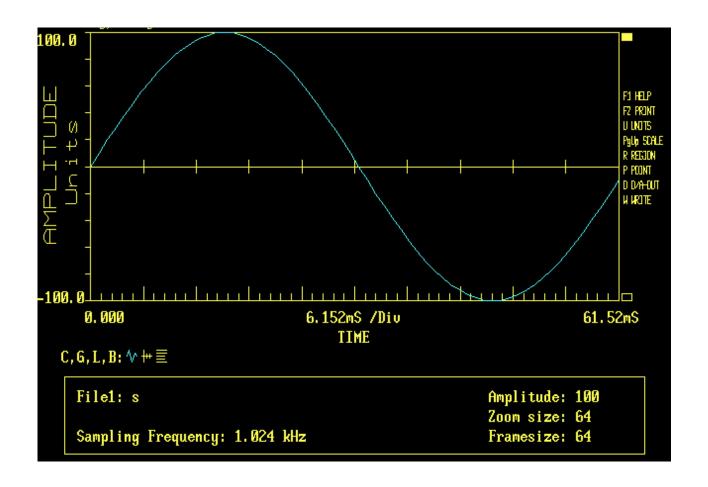
a. Nyquist rate sampling:  $f_s = 2 f$ 

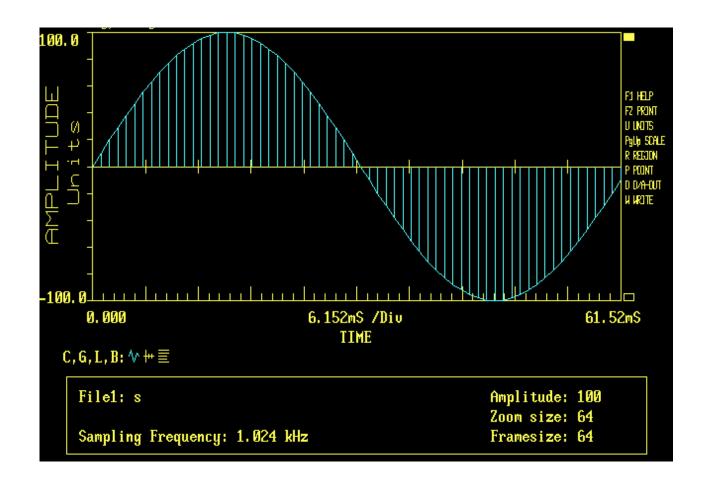


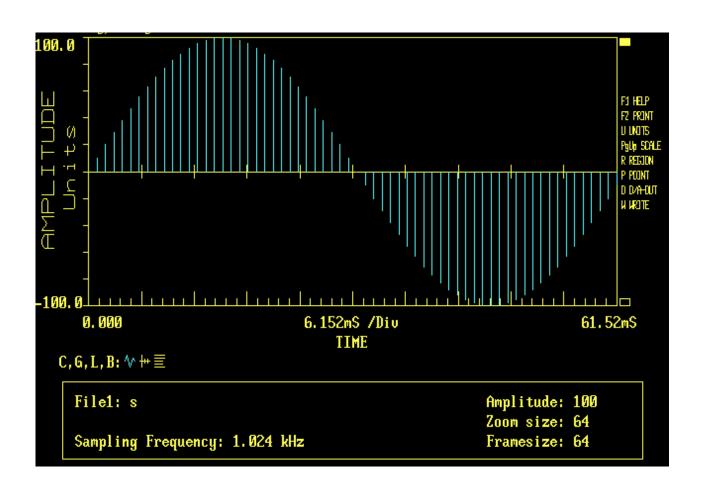
b. Oversampling:  $f_s = 4 f$ 



c. Undersampling:  $f_s = f$ 





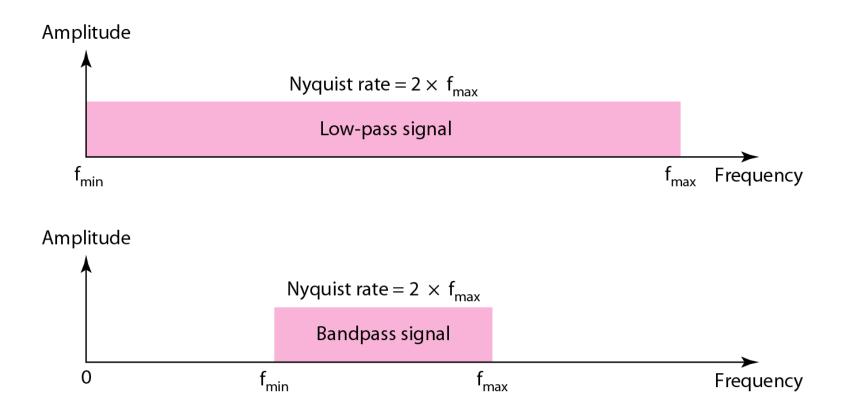


# Sampling Theorem

$$F_s \geq 2f_m$$

According to the Nyquist theorem, the sampling rate must be at least 2 times the highest frequency contained in the signal.

### Nyquist sampling rate for low-pass and bandpass signals



# Quantization

- Sampling results in a series of pulses of varying amplitude values ranging between two limits: a min and a max.
- The amplitude values are infinite between the two limits.
- We need to map the *infinite* amplitude values onto a finite set of known values.
- This is achieved by dividing the distance between min and max into L zones, each of height  $\Delta$ .

$$\Delta = (\max - \min)/L$$

## **Quantization Levels**

- The midpoint of each zone is assigned a value from 0 to L-1 (resulting in L values)
- Each sample falling in a zone is then approximated to the value of the midpoint.

## **Quantization Zones**

- Assume we have a voltage signal with amplitutes  $V_{min}$ =-20V and  $V_{max}$ =+20V.
- We want to use L=8 quantization levels.
- Zone width  $\Delta = (20 20)/8 = 5$
- The 8 zones are: -20 to -15, -15 to -10, -10 to -5, -5 to 0, 0 to +5, +5 to +10, +10 to +15, +15 to +20
- The midpoints are: -17.5, -12.5, -7.5, -2.5, 2.5, 7.5, 12.5, 17.5

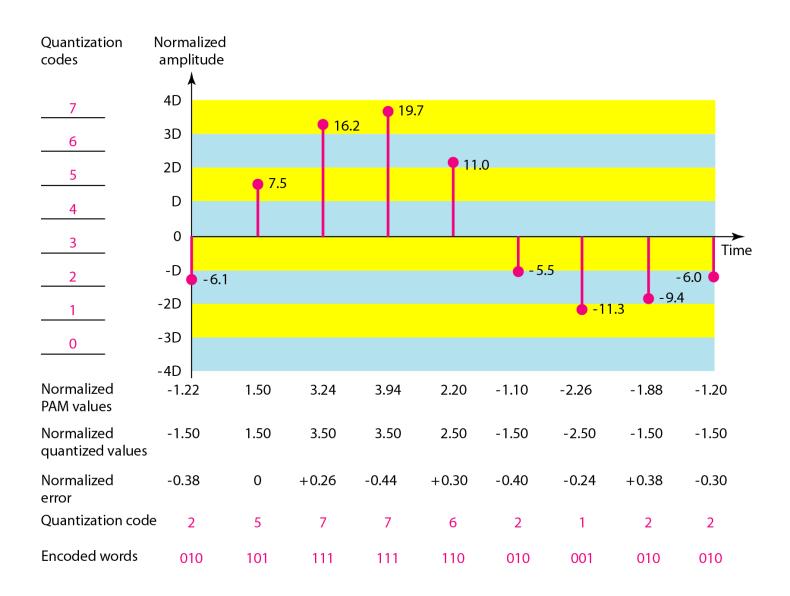
# **Assigning Codes to Zones**

- Each zone is then assigned a binary code.
- The number of bits required to encode the zones, or the number of bits per sample as it is commonly referred to, is obtained as follows:

$$n_b = log_2 L$$

- Given our example,  $n_b = 3$
- The 8 zone (or level) codes are therefore: 000, 001, 010, 011, 100, 101, 110, and 111
- Assigning codes to zones:
  - 000 will refer to zone -20 to -15
  - 001 to zone -15 to -10, etc.

## Quantization and encoding of a sampled signal



# **Quantization Error**

- When a signal is quantized, we introduce an error
  - the coded signal is an approximation of the actual amplitude value.
- The difference between actual and coded value (midpoint) is referred to as the quantization error.
- The more zones, the smaller  $\Delta$ 
  - which results in smaller errors.
- BUT, the more zones the more bits required to encode the samples
  - higher bit rate

## **Analog-to-digital Conversion**

**Example** An 12-bit analog-to-digital converter (ADC) advertises an accuracy of  $\pm$  the least significant bit (LSB). If the input range of the ADC is 0 to 10 volts, what is the accuracy of the ADC in analog volts?

#### **Solution:**

If the input range is 10 volts then the analog voltage represented by the LSB would be:

$$V_{LSB} = \frac{V_{\text{max}}}{2^{\text{Nu bits}}} = \frac{10}{2^{12}} = \frac{10}{4096} = .0024 \text{ volts}$$

Hence the accuracy would be  $\pm$  0.0024 volts.

# Sampling related concepts

- Over/exact/under sampling
- Regular/irregular sampling
- Linear/Logarithmic sampling
- Aliasing
- Anti-aliasing filter
- Image
- Anti-image filter

#### Steps for digitization/reconstruction of a signal

- Band limiting (LPF)
- Sampling / Holding
- Quantization
- Coding

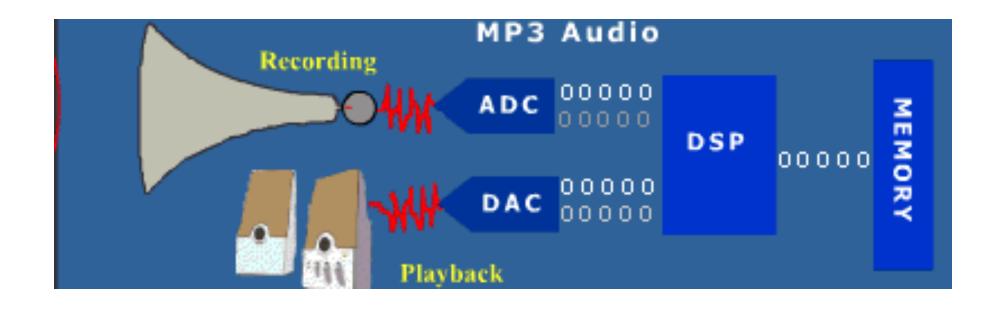
These are basic steps for A/D conversion

- D/A converter
- Sampling / Holding
  - Image rejection

These are basic steps for reconstructing a sampled digital signal

# Digital data: end product of A/D conversion and related concepts

- Bit: least digital information, binary 1 or 0
- Nibble: 4 bits
- Byte: 8 bits, 2 nibbles
- Word: 16 bits, 2 bytes, 4 nibbles
- Some jargon:
  - integer, signed integer, long integer, 2s
     complement, hexadecimal, octal, floating point, etc.



## Measures of capacity and speed in Computers

Special Powers of 10 and 2:

```
    Kilo- (K) = 1 thousand = 10<sup>3</sup> and 2<sup>10</sup>
    Mega- (M) = 1 million = 10<sup>6</sup> and 2<sup>20</sup>
    Giga- (G) = 1 billion = 10<sup>9</sup> and 2<sup>30</sup>
    Tera- (T) = 1 trillion = 10<sup>12</sup> and 2<sup>40</sup>
    Peta- (P) = 1 quadrillion = 10<sup>15</sup> and 2<sup>50</sup>
```

Whether a metric refers to a power of ten or a power of two typically depends upon what is being measured.

## **Example**

- Hertz = clock cycles per second (frequency)
  - -1MHz = 1,000,000Hz
  - Processor speeds are measured in MHz or GHz.
- Byte = a unit of storage
  - $1KB = 2^{10} = 1024$  Bytes
  - $1MB = 2^{20} = 1,048,576$  Bytes
  - Main memory (RAM) is measured in MB
  - Disk storage is measured in GB for small systems, TB for large systems.

## Measures of time and space

```
    Milli- (m) = 1 thousandth = 10<sup>-3</sup>
    Micro- (μ) = 1 millionth = 10<sup>-6</sup>
    Nano- (n) = 1 billionth = 10<sup>-9</sup>
    Pico- (p) = 1 trillionth = 10<sup>-12</sup>
    Femto- (f) = 1 quadrillionth = 10<sup>-15</sup>
```

# Data types

- Our first requirement is to find a way to represent information (data) in a form that is mutually comprehensible by human and machine.
  - Ultimately, we need to develop schemes for representing all conceivable types of information - language, images, actions, etc.
  - Specifically, the devices that make up a computer are switches that can be on or off, i.e. at high or low voltage.
  - Thus they naturally provide us with two symbols to work with:
    - we can call them on and off, or 0 and 1.

## What kinds of data do we need to represent?

#### Numbers

signed, unsigned, integers, floating point, complex, rational, irrational,...

#### Text

characters, strings, ...

#### **Images**

pixels, colors, shapes, ...

#### Sound

#### Logical

true, false

#### Instructions

. . .

#### Data type:

representation and operations within the computer

# Number Systems – Representation

- Positive radix, positional number systems
- A number with *radix r* is represented by a string of digits:

$$A_{n-1}A_{n-2} \dots A_1A_0 \cdot A_{-1}A_{-2} \dots A_{-m+1}A_{-m}$$
  
in which  $0 \le A_i < r$  and  $\cdot$  is the *radix point*.

• The string of digits represents the power series:

$$(Number)_{r} = \left(\sum_{i=0}^{i=n-1} A_{i} \cdot r^{i}\right) + \left(\sum_{j=-m}^{j=-1} A_{j} \cdot r^{j}\right)$$

$$(Integer Portion) + (Fraction Portion)$$

## **Decimal Numbers**

- "decimal" means that we have ten digits to use in our representation
  - the symbols 0 through 9
- What is 3546?
  - it is three thousands plus five hundreds plus four tens plus six ones.
  - i.e.  $3546 = 3 \times 10^3 + 5 \times 10^2 + 4 \times 10^1 + 6 \times 10^0$
- How about negative numbers?
  - we use two more <u>symbols</u> to distinguish positive and negative:
    - + and -

# **Unsigned Binary Integers**

$$Y = \text{"abc"} = a.2^2 + b.2^1 + c.2^0$$

(where the digits a, b, c can each take on the values of 0 or 1 only)

	N = number of bits		3-bits	5-bits	8-bits
	Range is:	0	000	00000	00000000
	$0 \le i \le 2^N - 1$	1	001	00001	00000001
Dualda la seco		2	010	00010	00000010
•	Problem: How do we represent negative numbers?	3	011	00011	00000011
		4	100	00100	00000100

# **Signed Binary Integers -2s Complement representation-**

- Transformation
  - To transform a into -a, invert all
     bits in a and add 1 to the result

#### **Advantages:**

- Operations need not check the sign
  - Only one representation for zero
    - Efficient use of all the bits

-16	10000
•••	•••
-3	11101
-2	11110
-1	11111
0	00000
+1	00001
+2	00010
+3	00011
•••	•••
+15	01111

# Limitations of integer representations

- Most numbers are not integer!
  - Even with integers, there are two other considerations:
- Range:
  - The magnitude of the numbers we can represent is determined by how many bits we use:
    - e.g. with 32 bits the largest number we can represent is about +/- 2 billion, far too small for many purposes.
- Precision:
  - The exactness with which we can specify a number:
    - e.g. a 32 bit number gives us 31 bits of precision, or roughly 9 figure precision in decimal repesentation.
- We need another data type!

## Real numbers

- Our decimal system handles non-integer *real* numbers by adding yet another symbol the decimal point (.) to make a *fixed point* notation:
  - e.g.  $3456.78 = 3.10^3 + 4.10^2 + 5.10^1 + 6.10^0 + 7.10^{-1} + 8.10^{-2}$
- The *floating point*, or scientific notation allows us to represent very large and very small numbers (integer or real), with as much or as little precision as needed:
  - Unit of electric charge  $e = 1.602 176 462 \times 10^{-19}$  Coulomb
  - Volume of universe =  $1 \times 10^{85} \text{ cm}^3$ 
    - the two components of these numbers are called the mantissa and the exponent

### Real numbers in binary

- We mimic the decimal floating point notation to create a "hybrid" binary floating point number:
  - We first use a "binary point" to separate whole numbers from fractional numbers to make a fixed point notation:
    - e.g.  $00011001.110 = 1.2^4 + 1.10^3 + 1.10^1 + 1.2^{-1} + 1.2^{-2} \Rightarrow 25.75$ (2<sup>-1</sup> = 0.5 and 2<sup>-2</sup> = 0.25, etc.)
  - We then "float" the binary point:
    - $00011001.110 \Rightarrow 1.1001110 \times 2^4$ mantissa = 1.1001110, exponent = 4
  - Now we have to express this without the extra symbols (x, 2, .)
    - by convention, we divide the available bits into three fields:

sign, mantissa, exponent

### IEEE-754 fp numbers - 1

s biased exp. fraction 23 bits 8 bits

 $N = (-1)^s \times 1.$ fraction  $\times 2^{(biased exp. - 127)}$ 

• Sign: 1 bit

**32 bits:** 

- Mantissa: 23 bits
  - We "normalize" the mantissa by dropping the leading 1 and recording only its fractional part (why?)
- Exponent: 8 bits
  - In order to handle both +ve and -ve exponents, we add 127 to the actual exponent to create a "biased exponent":
    - $2^{-127} =$  biased exponent = 0000 0000 (= 0)
    - $2^0 => biased exponent = 0111 1111 (= 127)$
    - $2^{+127} => biased exponent = 1111 1110 (= 254)$

### IEEE-754 fp numbers - 2

- Example: Find the corresponding fp representation of 25.75
  - $25.75 \Rightarrow 00011001.110 \Rightarrow 1.1001110 \times 2^4$
  - sign bit = 0 (+ve)
  - normalized mantissa (fraction) = 100 1110 0000 0000 0000 0000
  - biased exponent =  $4 + 127 = 131 \Rightarrow 1000\ 0011$
  - so  $25.75 \Rightarrow 0.1000\ 0011\ 100\ 1110\ 0000\ 0000\ 0000\ 0000 \Rightarrow x41CE0000$
- Values represented by convention:
  - Infinity (+ and -): exponent = 255 (1111 1111) and fraction = 0
  - NaN (not a number): exponent = 255 and fraction ≠ 0
  - Zero (0): exponent = 0 and fraction = 0
    - note: exponent = 0 => fraction is *de-normalized*, i.e no hidden 1

### IEEE-754 fp numbers - 3

• Double precision (64 bit) floating point

	S	biased exp.	fraction
64 bits:	1	11 bits	52 bits

$$N = (-1)^s \times 1.$$
fraction  $\times 2^{(biased exp. - 1023)}$ 

- Range & Precision:
  - 32 bit:
- mantissa of 23 bits + 1 => approx. 7 digits decimal
   2+/-127 => approx. 10+/-38
  - 64 bit:
- mantissa of 52 bits + 1 => approx. 15 digits decimal
   2+/-1023 => approx. 10+/-306

# **Binary Numbers and Binary Coding**

- Flexibility of representation
  - Within constraints below, can assign any binary combination (called a code word) to any data as long as data is uniquely encoded.

#### Information Types

- Numeric
  - Must represent range of data needed
  - Very desirable to represent data such that simple, straightforward computation for common arithmetic operations permitted
  - Tight relation to binary numbers
- Non-numeric
  - Greater flexibility since arithmetic operations not applied.
  - Not tied to binary numbers

## Non-numeric Binary Codes

- Given n binary digits (called <u>bits</u>), a <u>binary code</u> is a mapping from a set of <u>represented elements</u> to a subset of the  $2^n$  binary numbers.
- Example: A binary code for the seven colors of the rainbow
- Code 100 is not used

Color	<b>Binary Number</b>		
Red	000		
Orange	001		
Yellow	010		
Green	011		
Blue	101		
Indigo	110		
Violet	111		

## **Number of Bits Required**

• Given M elements to be represented by a binary code, the minimum number of bits, *n*, needed, satisfies the following relationships:

```
2^n > M > 2^{(n-1)}

n = \lceil \log_2 M \rceil where \lceil x \rceil, called the ceiling

function, is the integer greater than or equal to x.
```

- Example: How many bits are required to represent <u>decimal digits</u> with a binary code?
  - -4 bits are required  $(n = \lceil \log_2 9 \rceil = 4)$

### Number of Elements Represented

- Given n digits in radix r, there are  $r^n$  distinct elements that can be represented.
- But, you can represent m elements,  $m < r^n$
- Examples:
  - You can represent 4 elements in radix r = 2 with n = 2 digits: (00, 01, 10, 11).
  - You can represent 4 elements in radix r = 2 with n = 4 digits: (0001, 0010, 0100, 1000).

## **Binary Coded Decimal (BCD)**

- In the 8421 Binary Coded Decimal (BCD) representation each decimal digit is converted to its 4-bit pure binary equivalent
- This code is the simplest, most intuitive binary code for decimal digits and uses the same powers of 2 as a binary number,
  - but only encodes the first ten values from 0 to 9.
    - For example:  $(57)_{dec} \rightarrow (?)_{bcd}$

### **Error-Detection Codes**

- Redundancy (e.g. extra information), in the form of extra bits, can be incorporated into binary code words to detect and correct errors.
- A simple form of redundancy is <u>parity</u>, an extra bit appended onto the code word to make the number of 1's odd or even.
  - Parity can detect all single-bit errors and some multiple-bit errors.
- A code word has even parity if the number of 1's in the code word is even.
- A code word has odd parity if the number of 1's in the code word is odd.

## 4-Bit Parity Code Example

• Fill in the even and odd parity bits:

Even Parity Message- Parity	Odd Parity Message_ Parity
000_	000_
001_	001_
010_	010_
011_	011_
100_	100_
101_	101_
110_	110_
111 _	111 _

• The codeword "1111" has <u>even parity</u> and the codeword "1110" has <u>odd parity</u>. Both can be used to represent 3-bit data.

### **ASCII Character Codes**

- American Standard Code for Information Interchange
- This code is a popular code used to represent information sent as character-based data.
- It uses 7- bits to represent
  - 94 Graphic printing characters
  - 34 Non-printing characters
- Some non-printing characters are used for text format
  - e.g. BS = Backspace, CR = carriage return
- Other non-printing characters are used for record marking and flow control
  - e.g. STX = start text areas, <math>ETX = end text areas.

### **ASCII Properties**

- ASCII has some interesting properties:
- Digits 0 to 9 span Hexadecimal values  $30_{16}$  to  $39_{16}$
- Upper case A-Z span 41<sub>16</sub> to 5A<sub>16</sub>
- Lower case a-z span  $61_{16}$  to  $7A_{16}$ 
  - Lower to upper case translation (and vice versa) occurs by flipping bit 6
- Delete (DEL) is all bits set,
  - a carryover from when punched paper tape was used to store messages

#### UNICODE

- UNICODE extends ASCII to 65,536 universal characters codes
  - For encoding characters in world languages
  - Available in many modern applications
  - − 2 byte (16-bit) code words

### Warning: Conversion or Coding?

- Do NOT mix up "conversion of a decimal number to a binary number" with "coding a decimal number with a binary code".
- $13_{10} = 1101_2$ 
  - -This is conversion

- 13  $\Leftrightarrow$  0001 0011<sub>BCD</sub>
  - -This is coding

### Another use for bits: Logic

#### Beyond numbers

- logical variables can be true or false, on or off, etc., and so are readily represented by the binary system.
- A logical variable A can take the values false = 0 or true = 1 only.
- The manipulation of logical variables is known as Boolean Algebra, and has its own set of operations
  - which are not to be confused with the arithmetical operations.
- Some basic operations: NOT, AND, OR, XOR

## **Basic Logic Operations**

Truth Tables of Basic Operations

NOT	<u>AND</u>	<u>OR</u>		
<u>A</u> <u>A'</u>	<u>A</u> <u>B</u> <u>A.B</u>	<u>A</u> <u>B</u> <u>A+B</u>		
0 1	0  0  0	0 0 0		
1 0	0 1 0	0 1 1		
_	1 0 0	1 0 1		
	1 1 1	1 1 1		

- Equivalent Notations
  - $\text{ not } A = A' = \overline{A}$
  - -A and  $B = A.B = A \land B = A$  intersection B
  - $-A \text{ or } B = A+B = A \vee B = A \text{ union } B$

## **More Logic Operations**

<u>XOR</u>			XNOR			
<u>A</u>	<u>B</u>	<u>A⊕B</u>	_	<u>A</u>	<u>B</u>	<u>(A⊕B)'</u>
0	0	0		0	0	1
0	1	1		0	1	0
1	0	1		1	0	0
1	1	0		1	1	1

- Exclusive OR (XOR): either A or B is 1, not both
- $-A \oplus B = A.B' + A'.B$